







Multi-task group Lasso for Genome Wide Association Studies in admixed populations

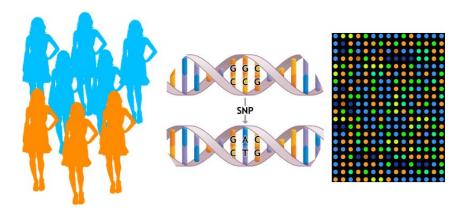
Asma Nouira Chloé-Agathe Azencott

MINES ParisTech, CBIO-Centre for Computational Biology, Institut Curie, INSERM, U900, PSL Research University

ISMB 2021 MLCSB COSI

July 29th 2021

Genome Wide Association Studies



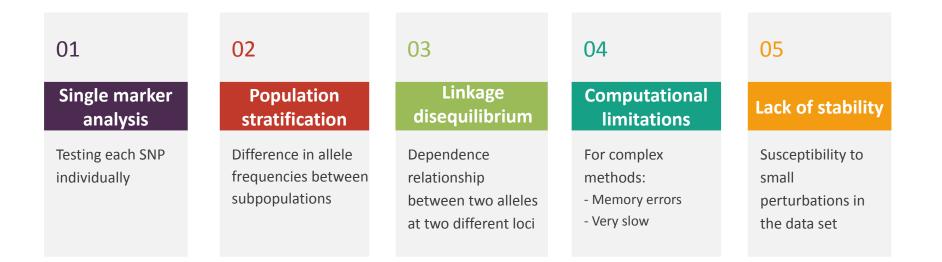
Goal: Find association between the genotype and the phenotype.

- The genotype: Single Nucleotide Polymorphism (SNP) arrays.
- The phenotype:
 - Quantitative: BMI, weight, height, etc.
 - Qualitative: Case-control study

Challenges in GWAS analysis

• Microarray data: SNP arrays

Curse of dimensionality (p>>N): $p \approx 10^5 - 10^7$, $N \approx 10^2 - 10^4$



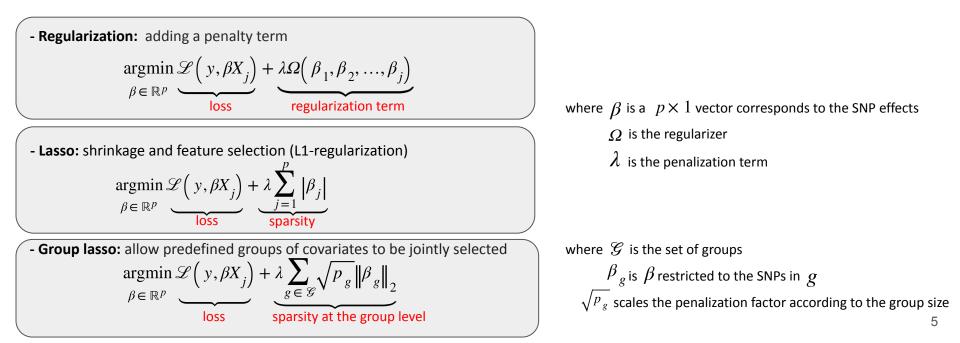
01	02	03	04	05
Single-marker analysis	Population stratification	Linkage disequilibrium	Computational limitation	Lack of stability
Testing each SNP individually	Difference in allele frequencies between subpopulations	Dependence relationship between two alleles at two different loci	For complex methods: - Memory errors - Very slow	Susceptibility to small perturbations in the data set

• Single-marker analysis:

Given a phenotype y, X is the genotype matrix:

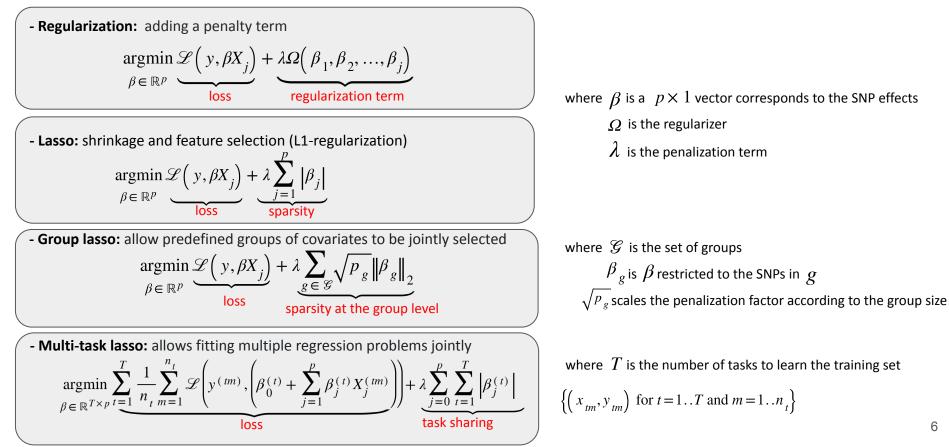
For each feature \mathbf{X}_{j} , we fit a single-predictor equation $\mathbf{y} = \boldsymbol{\beta}_{0} + \boldsymbol{\beta}_{j} \mathbf{X}_{j} + \varepsilon \Rightarrow$ p-value from a t-test against an intercept-only model $H_{0} = \left\{ \boldsymbol{\beta}_{j} = 0 \right\}$.

• Multi-variate approach: Feature selection based on regularization



From GWAS to Machine Learning

• Multi-variate approach: Feature selection based on regularization



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Population stratification refers to the presence of differences in allele frequencies between subpopulations due to different ancestry.

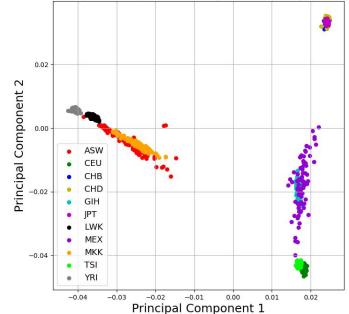
- State-of-the art adjustment methods
 - PCA-based methods

Include Principal components (PCs) as covariates

- Logistic Regression + Top PCs^[1,2]
- EIGENSTRAT^[3]: multi-linear regression + 10 PCs
- Linear mixed models

^[1]Need et al., A genome-wide investigation of snps and cnvs in schizophrenia. 2009, *PLoS Genet*.

^[2]Zeggini et al., Meta-analysis of genome-wide association data and large-scale replication identifies additional susceptibility loci for type 2 diabetes. 2008, Nat Genet.



Principal Component Analysis - HapMap3 data

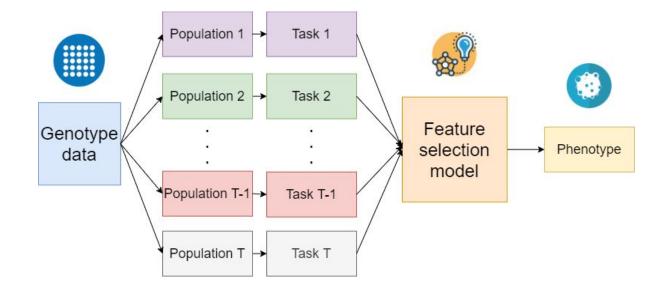
Fast-LMM^[4]

^[3]Price et al., Principal components analysis corrects for stratification in genome-wide association studies. *Nat Genet*.

^[4]Lippert et al., FaST linear mixed models for genome-wide association studies. 2011. Nat Methods.

Population stratification

• **Proposed adjustment method**: subpopulations assignment in multitask framework



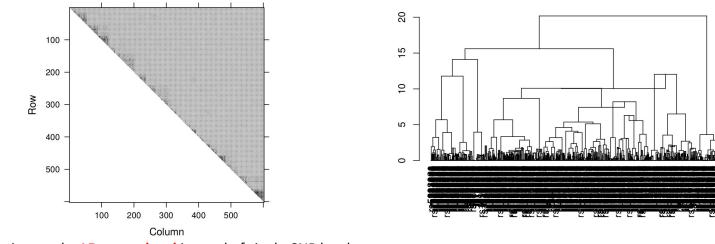
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Linkage Disequilibrium (LD):

- Tendency of alleles to be transmitted together, more often that expected by chance alone.
- Usually caused by close proximity of genes in the same chromosome.

Hierarchical clustering approach^[1]

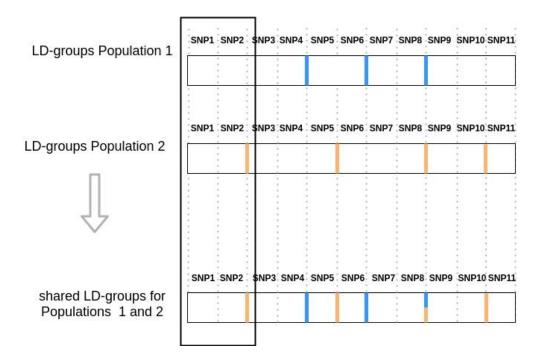
Performing a spatially-constrained hierarchical clustering



⇒ Selection on the LD-group level instead of single-SNP level.

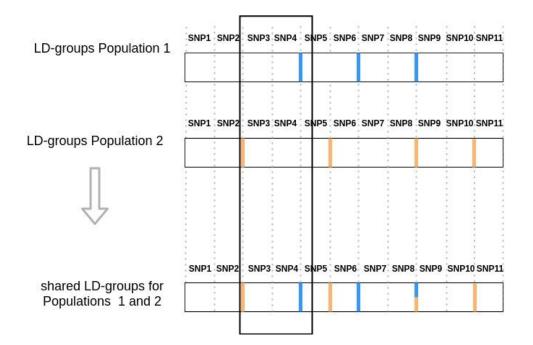
• Choice of LD-groups

Linkage disequilibrium is different in different populations



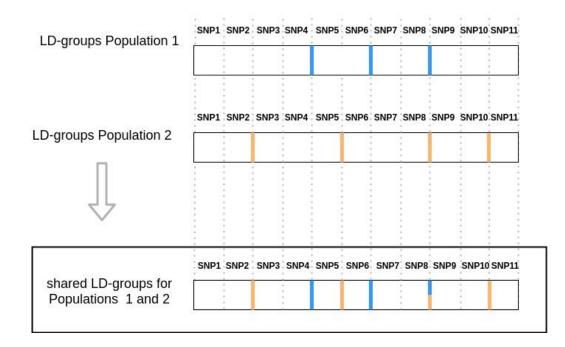
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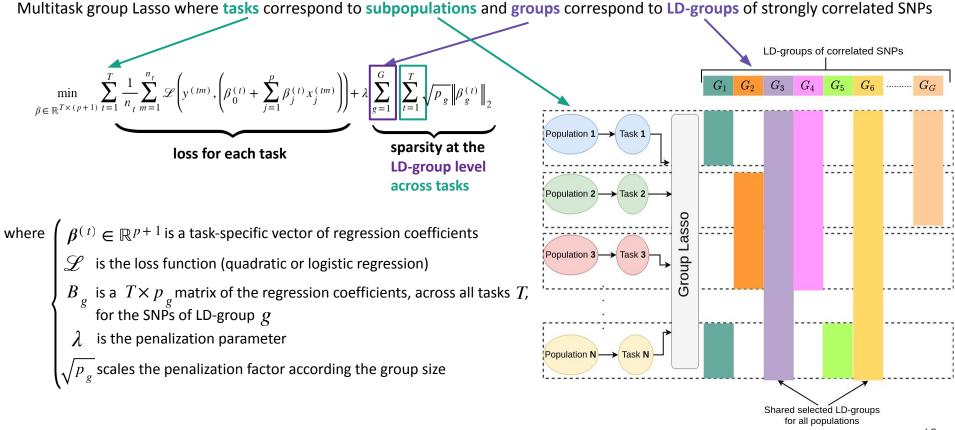
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⇒ Selection of LD-groups associated with the phenotype across all tasks/populations, or specifically for some tasks/populations

			04	
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Gap Safe screening rules

Gap Safe Screening rules^[1]**:** eliminates features with associated coefficients are proved to be zero at the optimum in order to obtain **more speed up** and to **avoid memory errors**.

Ignoring some variables by exploiting geometric properties of the dual formulation of the following optimization problem:

$$\widehat{\beta}^{(\lambda)} \in \underset{\beta \in \mathbb{R}^{p}}{\operatorname{argmin}} P_{\lambda}(\beta), \text{ for } P_{\lambda}(\beta) := F(\beta) + \lambda \Omega(\beta) := \sum_{i=1}^{n} f_{i}(x_{i}^{\top}\beta) + \lambda \Omega(\beta)$$

where $f_i: \mathbb{R} \mapsto \mathbb{R}$ are convex and differentiable functions and $\Omega: \mathbb{R}^p \mapsto \mathbb{R}_+$ is a group-decomposable norm: $\Omega(\beta) = \sum_{g \in \mathcal{G}} \Omega_g(\beta_g)$ with Ω_p a norm of \mathbb{R}^{n_g}

For group Lasso: the data fitting term is $F(\beta) = \frac{\mathscr{L}(y, \beta X_j)}{2}$,

The *L1/L2-norm* is defined by $\Omega(\beta) = \Omega_{W}(\beta)$:

$$\Omega_{w}(\beta) := \sum_{g \in \mathcal{G}} w_{g} \|\beta_{g}\|_{2} \quad \text{and} \quad \Omega_{w}^{D}(\xi) := \max_{g \in \mathcal{G}} \frac{\|\xi_{g}\|_{2}}{w_{g}}$$

where $w = (w_g)_{g \in \mathcal{G}}$ are weights satisfying $w_g > 0$ for all $g \in \mathcal{G}$ and $\Omega^D_w(\xi)$ is the dual norm along the regularization path.

^[1]Ndiaye et al., Gap Safe Screening Rules for Sparsity Enforcing Penalties. 2017, *Journal of Machine Learning Research 18*.

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Stability Selection

Stability selection^[1]**: bootstrap aggregation** procedure where feature selection is performed repeatedly on bootstrap subsamples, and the results of all repetitions are aggregated. It allows a **precise statement** of the significance of the selected features set and **reduce false positives**.

Procedure:

- Identify $S = \{k: \beta_k \neq 0\}$ a set of non-zero inputs of a sparse parameter vector β of observed data (X, y)
- Feature selection is performed on randomly $|I| = \frac{n}{2}$ of observations, where $I \subset \{1, ..., n\}$
- Selection Path: Probability of the selection of a feature $k \in \{1, ..., p\}$

 $\pi_k^{\lambda} = Pr^* \left[k \in \widehat{S}^{\lambda}(I) \right]$, where $\widehat{S}^{\lambda}(I) \subset \{1, ..., p\}$ denotes the selected features by a subsample I

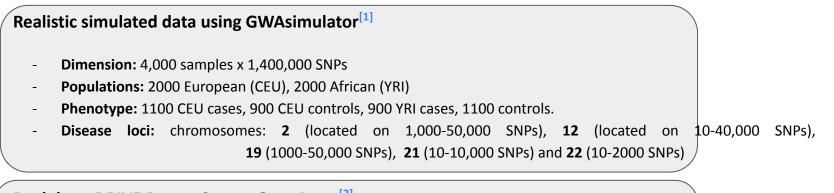
- ⇒ Captures random selection within feature selection algorithms
- For a chosen cut-off $\frac{1}{2} \le \pi_{thre} \le 1$, the set of stable features is:

$$\widehat{S}^{stable} = \left\{ k \colon \pi_k^{\lambda} \ge \pi_{thre} \right\}$$

 \Rightarrow Only variables that are selected consistently across all the random halves remain.

^[1]Meinshausen et al,. Stability selection. 2010. Journal of the Royal Statistical Society Series B-Statistical Methodology.

• Datasets



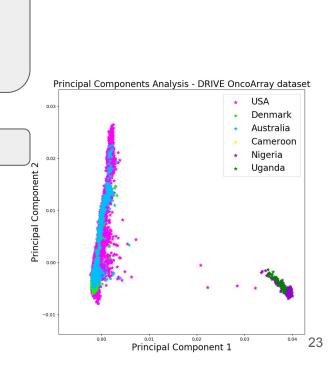
Real data: DRIVE Breast Cancer OncoArray^[2]

- **Dimension:** 28,281 samples x 528,620 SNPs
- Phenotype: 13,846 cases and 14,435 controls
- **Populations:** USA Uganda Nigeria Cameroon Australia Denmark

- Quality control and preprocessing
 - MAF < 5%
 - HWE-P-Value < 0.0001
 - Remove samples with missing case/control criterion
 - Sex check
 - Remove samples and/or variants with high genotypic missing rate
 - Imputation of missing values: IMPUTE2

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- Subpopulations definition

Assign subpopulations in Multitask framework according to PCA patterns



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- Evaluation of Multi-task group Lasso
 - Validation using simulated data

Generate simulations with specified multi locus disease model in specified regions

- ⇒ Compute false positives rate
 - Estimation of the stability of the selection ^[1,2]

 $Stability = \widehat{\Phi}(s_1, s_2, \dots s_M) = \frac{1}{M(M-1)} \sum_i \sum_{i \neq i} sim(s_i, s_j)$

• Comparison with the state-of-the art methods

^[1]Kuncheva et Al., A stability index for feature selection. 2008, *IASTED International Conference on Artificial Intelligence and Applications*. ^[2]Nogueira et Al., On the Stability of Feature Selection Algorithms. 2018, *Journal of Machine Learning Reasearch 18*.

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- Lasso after PCA adjustment for population stratification at the SNP level
- 2. Group Lasso after PCA adjustment for population stratification at LD-groups level
- 3. Separate group Lasso for each subpopulation at LD-groups level
- 4. Separate Lasso for each

subpopulation at the SNP level

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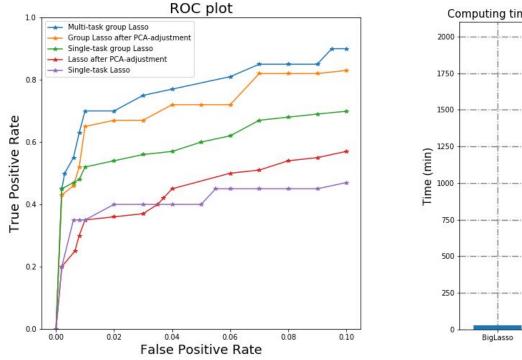
$$Stability = \widehat{\Phi}(s_1, s_2, \dots s_M) = \frac{1}{M(M-1)} \sum_{i=1}^{N} \sum_{j=1}^{N} sim(s_i, s_j)$$

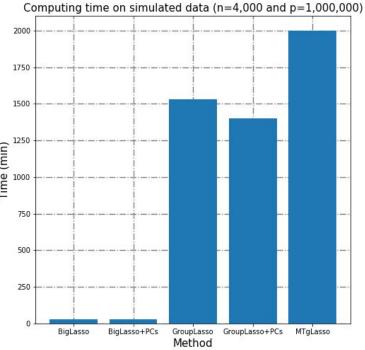
- Comparison with the state-of-the art methods \overline{i} $\overline{j \neq i}$
- Computational time

^[1]Kuncheva et Al., A stability index for feature selection. 2008, *IASTED International Conference on Artificial Intelligence and Applications*. ^[2]Nogueira et Al., On the Stability of Feature Selection Algorithms. 2018, *Journal of Machine Learning Reasearch 18*.

Results of Multitask group Lasso and comparison

Multitask group Lasso outperforms the state-of-the-art methods on simulated data



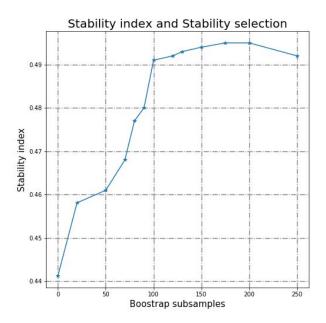


Multitask group Lasso results and comparison

Multitask group Lasso is more stable than the state-of-the-art methods.

Simulated data: n=4,000 ; p=1,000,000 ; LD-groups number = 35,792 groups

Methods	Number of selected features/groups	Stability index	Selection level
Multi-task group Lasso (100 boostraps)	5,623	0.4912	LD-groups level
Group Lasso after PCs adjustment	6,054	0.4134	LD-groups level
Single task group Lasso	4,836	0.3398	LD-groups level
Lasso after PCs adjustment	158,856	0.2368	Single-SNP level
Single task Lasso	168,158	0.1742	Single-SNP level



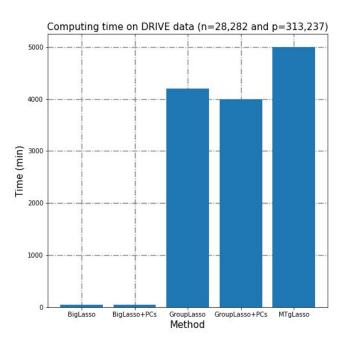
 \Rightarrow The feature selection at the LD-groups level alleviate the curse of dimensionality and the lack of stability.

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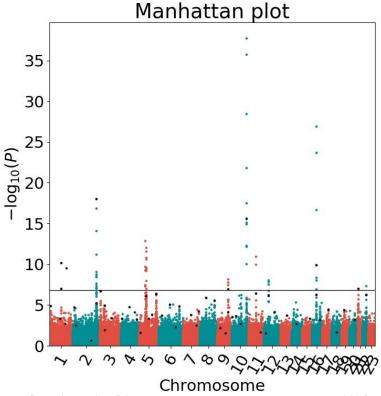
Real data: DRIVE Breast Cancer OncoArray^[1] n=28,282 ; p=313,237 ; LD-groups number = 17,782 groups

Methods	Number of selected features/groups	Stability index	Selection level
Multi-task group Lasso (100 boostraps)	62	0.4312	LD-groups level
Group Lasso after PCs adjustment	59	0.3234	LD-groups level
Single task group Lasso	58	0.2498	LD-groups level
Lasso after PCs adjustment	874	0.2068	Single-SNP level
Single task Lasso	789	0.1581	Single-SNP level

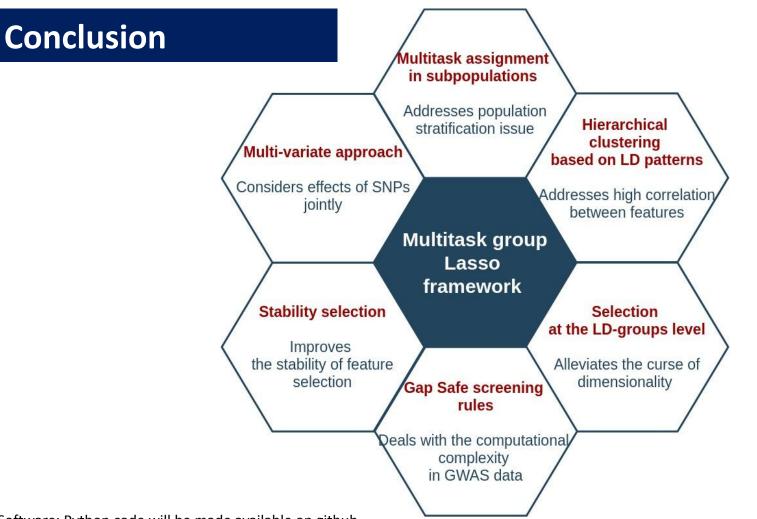


Multitask group Lasso results and comparison

Real data: DRIVE Breast Cancer OncoArray^[1] n=28,282 ; p=313,237 ; LD-groups number = 17,782 groups



Black dots corresponds to Multitask group Lasso **discoveries** (one SNP per LD-group is represented in the Manhattan plot)



Software: Python code will be made available on github.

Acknowledgements

- CBIO (Mines ParisTech)
- GWAS team
- U900 (Institut Curie)
- This work was supported in part by Agence Nationale de la Recherche (ANR-18-CE45-0021-01 and ANR19-P3IA-0001)



Postdoc openings on GWAS & ML at CBIO! Talk to Chloé



Thank you

Poster session

29th July 15:20 à 16:20